# Mark scheme

Qu	esti	on	Answer/Indicative content	Marks	Guidance		
1	а		Angle in a semi-circle [= 90]	1		Accept: Angle subtended by diameter [ = 90] Angle at centre is twice angle at circumference	
	b		EBD or EBO or FBD or FBO and angle between radius and tangent [= 90]	2	<b>B1</b> for EBD or EBO or FBD or FBO or for correct reason	Accept DBE etc but not B  Accept diameter for radius	
	С		43	1			
	d		29	1			
			Total	5			
2	а		45	2	M1 for 360 ÷ 8 or for 180 – $\frac{180 \times (8-2)}{8}$ oe		
	b		135	1	Correct or <b>FT</b> 180 – their 45	<b>FT</b> dep on (a) < 180	
			Total	3			
3	а		84	3	<b>B1</b> for angle SRQ = 180 – 54 or SRQ = 126 <b>B1</b> for angle RSQ = 42 <b>B1</b> for angle ROQ =	Could be marked on the diagram, For alternative methods refer to 'Qn12a, 2024 June, Alternative J560/04, Mark Scheme Appendix'	

				2 × <i>their</i> 42 to maximum of <b>B2</b>	within downloadable resource materials.
	b	Method 1 using angle EFH:  angle DEF = angle EFH because alternate [angle]  angle EDF = angle EFH because alternate segment [thm.]  therefore angle DEF = angle EDF or "they have two angles equal" oe	B1 B1 B1dep	Method 2 using angle DFG:  angle EDF = angle DFG because alternate [angle]  angle DEF = angle DFG because alternate segment [theorem]  dep on B2 awarded  If 0 scored SC1 for two sets of angles linked with incorrect/missing reasons e.g. DEF = EFH and EDF = EFH or EDF = DFG and DEF = DFG	If extra statements mark the best two  BOD 'alternating' but not 'Z-angles'  BOD 'alt. seg.'  Note: Angles may be written the other way round e.g. EDF is the same as FDE and they can say angle DFG = angle EDF and in marking you must use either method 1 or method 2 not both
		Total	6		
4		16 <b>nfww</b>	4	<b>B2</b> for 22.5 <b>M1</b> for 360 ÷ their 22.5 seen OR <b>B1</b> for 7a and a or 8a <b>M1</b> for 7a + a = 180 <b>oe</b> <b>M1</b> for 360 ÷ their 22.5 seen Alternative method 1: <b>M2</b> for 7 × 360 = 180(n - 2) or better or <b>M1</b> for $\frac{180(n-2)}{n} = 7 \times \frac{360}{n}$ and <b>M1</b> for 180n = 2520 + 360 <b>oe</b>	Alternative for number of sides: e.g. <b>M1</b> for $\frac{180(n-2)}{n} = 180 - their 22.5$

				Alternative method 2: Use of trials by choosing a value for $n$ .  M1 for each correct trial up to a maximum of M3 for using two of these [exterior angle] = $\frac{360}{n}$ (formula A) [interior angle] = $\frac{180(n-2)}{n}$ (formula B interior + exterior = 180 and for checking that interior = 7 × exterior  if 0 scored SC1 for one of formula A or B seen or used	be seen from a calculation or a list.  See Appendix* for likely results  *Refer to 'Qn6, 2024 June,
		Total	4		
5		Acceptable bisector of angle C with two pairs of supporting arcs  Region above their bisector shaded	M2 B1	M1 for acceptable bisector of angle C with no or incorrect arcs  Dep on ruled line from angle C reaching AB	Tolerance ± 2° Accept dashed or solid line for bisector If additional incorrect bisectors are drawn then this is choice and M0 unless the shading indicates they have chosen the correct bisector  Accept any clear indication for shading
		Total	3		
6		Bar for 10-20 drawn with height 7 small squares	2	<b>M1</b> for 14 ÷ 10 <b>soi</b> by 1.4	Condone good freehand
		Total	2		
7	а	Angle in a semi-circle [= 90]	1	Examiner's Comments	Accept: Angle subtended by diameter [ = 90] Angle at centre is twice angle at circumference

Very few candidates used the conterminology in their reason. Commendates were, it is a right-angle, in angled triangle, or it is on the diameter.  B1 for EBD or EBO or FBD or FBD or FBD or FBD.	mon incorrect it is a right- meter.
B1 for EBD or EBD or   but r	
B1 for EBD or EBD or   but r	
	ept DBE etc not B
	ept diameter adius
EBD or EBO or FBO	
and Examiner's Comments	
b angle between radius and tangent [= 90]  2 Some candidates could identify a degree angle although angle ABC common error.	
Most did not give a complete exp the correct terminology in their re sometimes included the word tan but not both. Some candidates in that angle ABC was 90-degrees, was an angle in a semicircle.	ason. Reasons gent or radius, correctly stated
c 35 Examiner's Comments	
A few candidates answered this particle of the most common answers were 90. A common misconception is the AD and BC are parallel.	25, 45, 60 and
d 25 1 Examiner's Comments	
A few candidates answered this process common misconception is that an equal to angle EBA.	•
Total 5	
8 a 60 2	

				M1 for 360 ÷ 6  or for $\frac{180 - \frac{180 \times (6-2)}{6}}{6}$ oe
				Examiner's Comments  Those candidates that recognised the exterior sum of a polygon was 360° were usually successful in this part. For many candidates there were a number of misconceptions, however. These included interior angle sum of a polygon = 360, interior angle + exterior angle = 360. Some candidates attempted to find the interior angle first using \( \frac{180(6-2)}{6} \) and then subtracting from 180°, this was a less successful approach.
	р	120	1	Correct or FT 180 – their 60  Examiner's Comments  More candidates were successful in this part. Examiners allowed a follow through from the previous answer. A number did 360 minus their answer and some gave an interior angle sum of the polygon rather than the size of one individual angle.  Misconception  A number of candidates are not secure in recalling interior and exterior angle facts, e.g. common errors included exterior + interior = 360, interior angle sum = 360. Some did not recognise a hexagon has six sides.
		Total	3	
9		9.40 or 9.397 to 9.398	4	Accept 9.4 with working  B1 for [ABC =] 85 soi  AND  Accept 9.4 with working  May be seen on diagram or within M2/M1 expressions

				M2 for [AC =] $\frac{8 \times \sin(85 \text{ or their ABC})}{\sin 58}$ Or $\frac{\text{M1 for}}{\sin(85 \text{ or their ABC})} = \frac{8}{\sin 58} \text{ oe}$	
		Total	4		
10	а	BF = DE or BF = 4 <i>t</i> and [opposite sides of a] rectangle [are equal]  AB = BF [= 4 <i>t</i> ] and radii [of a sector/circle]	1 1	For <b>2 marks</b> , 4 <i>t</i> must be seen in at least one statement as BF or on the diagram as BF	
	b	ABF = 65 and BC = 2 $t$ $\frac{their 65}{360} \times 2\pi \times their 4t$ $\frac{25}{360} \times 2\pi \times 2t$ $4t + 2t + 4t + 2t$ $\frac{25}{360} \times 2\pi \times 2t + \frac{65}{360} \times 2\pi \times 4t$ $+4t + 2t + 4t + 2t$ $\frac{31}{18}\pi t + 12t$	B1 M1 M1 M1 A1		Stated or seen on diagram  All <b>M</b> marks may be seen within a summarising expression  Condone 8t + 4t, 6t + 6t etc but not 12t
		Total	7		
11		ABF 60 equilateral/all angles equal  FBC 120 straight line/line adds to 180  ECD 60 equilateral/all angles equal  BCF 30 FCE 90° and straight line/line adds to 180° angles in a triangle  BFC 30 triangle BCF is isosceles with BC = BF]	1 1 1 1	If <b>0</b> or <b>1</b> scored, instead award <b>SC2</b> for all of these angles correct  If <b>0</b> scored, instead award <b>SC1</b> for two of the first four angles correct	Ignore other angles Accept in any order Condone spelling Angles could be seen on diagram in correct position(s)  For full marks, must be convinced they are working forwards and not backwards

		Total	5		
12		BMD and [diameter bisects chord] so CD [diameter] is perpendicular to AB [chord]  [MD is] common  SAS	1 1 1		Also accept DMB  Accept e.g. 'shared'
		Total	3		
13	а	95	4	M1 for 5x - 160 = 2(x + 25) oe M1 for 5x - 160 = 2x + 50 FT their 4 term linear equation with brackets M1 for x = 70 FT their 4 term linear equation	FT linear equation with more than 4 terms but not fewer, must have at least two terms in x
	b	85 and Opposite angles of a cyclic quadrilateral are supplementary	2	FT 180 – their (a) B1 for 85 FT or for correct reason	Accept [Opp angles of] cyclic quad [add up to 180] [Angles in] opposite segments [are supplementary] Accept complete longer reasons Angles at a point add to 360 and angle at centre is twice angle at circumference oe  Any incorrect statement does not score for reason
		Total	6		
14		Bar for 30–45 drawn with height 3 small squares	2	M1 for 9 ÷ 15 soi by 0.6  Examiner's Comments  Those candidates who is density of 3.2 in part (a) correctly. A bar of height very common from cand	dentified a frequency usually drew this bar

				marks in part (a).	
				It was rare to see any wo 15 ÷ 9 was nearly as freq	
		Total	2		
15		acceptable bisector of angle A with two pairs of supporting arcs	M2 B1	M1 for acceptable bisector of angle A with no or incorrect arcs  Dep on ruled line from angle A reaching BC	Tolerance ± 2° Use overlay Accept dashed or solid line for bisector If additional incorrect bisectors are drawn then this is choice and M0 unless the shading indicates they have chosen the correct bisector  Accept any clear indication for shading
		Region to the left of their bisector shaded			
				Many recognised that the involved constructing the and shading to the left of attempted this gave an action and earned full marks. Enthe perpendicular bisecto length) as well as drawing the midpoint of BC.	bisector of angle BAC the bisector; most who ccurate construction rors included drawing r of BC (or another
		Total	3		
16		32 nfww	4	B2 for 11.25 M1 for 360 ÷ their 11.25 seen OR B1 for 15a and a or 16a M1 for 15a + a = 180 oe M1 for 360 ÷ their 11.25 seen  Alternative method 1: M2 for 15 × 360 = 180(r) - 2) or better or M1 for 150(r) = 15 × 360/n	consistent single letter <b>B1 M1</b> implied by $16a = 180 \text{ or } \frac{180}{15+1} \text{ oe}$ Alternative for number of sides: e.g. <b>M1</b> for $\frac{1800(n-2)}{n} = 180 - their 11.25$

and **M1** for 180*n* = 5400 + 360 oe

Alternative method 2:
Use of trials by choosing a value for *n*.

M1 for each correct trial up to a maximum of
M3 for using two of these

[exterior angle] =  $\frac{360}{n}$  (formula A)

[interior angle] =  $\frac{180(n-2)}{n}$ (formula B) interior + exterior = 180 and for checking that interior = 15 × exterior

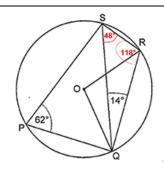
if **0** scored **SC1** for one of formula A or B seen or used

If they get 32 from any number of trials they score **4** marks. Trials can be seen from a calculation or a list.

see appendix for likely results

			1		
sides	interior	exterior			
5.00	108.00	72.00	35.00	169.71	10.29
6.00	120.00	60.00			
7.00	128.57	51.43			
8.00	135.00	45.00			
9.00	140.00	40.00			
10.00	144.00	36.00			
11.00	147.27	32.73			
12.00	150.00	30.00			
13.00	152.31	27.69			
14.00	154.29	25.71			
15.00	156.00	24.00			
16.00	157.50	22.50			
17.00	158.82	21.18			
18.00	160.00	20.00			
19.00	161.05	18.95			

	Total	4	11.25° a not kno sides. S interior 2). Few	correctly f and the ir w how to Some tho angle of seemed	ound the enterior ang use these ught the fo	exterior angle of gle of 168.75° but did eto find the number of ormula to find the polygon was 180(n – ne formula 360 ÷ n.
			11.25° a not kno sides. S interior	correctly found the inverse th	ound the enterior ang use these ught the fo	ple of 168.75° but did to find the number of ormula to find the polygon was 180( <i>n</i> –
			11.25° a not kno sides. S interior	correctly found the inverse th	ound the enterior ang use these ught the fo	ple of 168.75° but did to find the number of ormula to find the polygon was 180( <i>n</i> –
			Many for attempt exterior	ed it as if angle su	difficult. A the interior or to 360°	large number or angle and the and not 180°,
			23.00	164.35	15.65	
			21.00	162.86 163.64	17.14	
			20.00	162.00	18.00	



Hence angle ROQ = 96° from which ORQ=OQR=42°, SRO=76°, OQS=28°.

## Alternative method 1

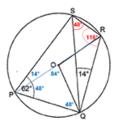
Some candidates are joining OP, however ROP are not co-linear but point P can be moved so that ROP is a straight line and maintaining angle SPQ as 62°.

Mark this;

**B1** for angle SPO = 14°

**B1** for angle OPQ and angle OQP = 48°

**B1** for angle QOP = 84° or OQR and ORQ = 42° to maximum of **B2** 



#### Alternative method 2

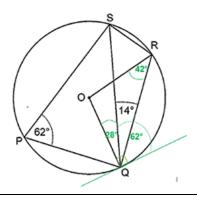
They can draw a tangent at Q. T is the end of the tangent.

B1 for SQT =  $62^{\circ}$  (alternate segment theorem),

B1 for (angle OQT =  $90^{\circ}$ ) so angle OQS =  $28^{\circ}$ ,

B1 for making angle OQR = 42° = angle ORQ. to maximum of B2

Hence angle ROQ =  $180^{\circ} - 42^{\circ} - 42^{\circ} = 96^{\circ}$ 



				Examiner's Comments  On the diagram, we often a written as 118° and the an correctly, but with some of calculated. Only a few can calculate the correct answer answer or showed a few in highlighting that the angle within a circle continues to candidates struggle with.	gle RSQ as 48° her angles incorrectly didates were able to er. Most did not acorrect angles, properties of lines
	р	Method 1 using angle EFH:  angle DEF = angle EFH because alternate [angle]  angle EDF = angle EFH because alternate segment [thm.]  therefore angle DEF = angle EDF or "they have two angles equal" oe	B1 B1 B1dep	Method 2 using angle DFG:  angle EDF = angle DFG because alternate [angle]  angle DEF = angle DFG because alternate segment [theorem]  dep on B2 awarded  If 0 scored SC1 for two sets of angles linked with incorrect/missing reasons e.g. DEF = EFH and EDF = EFH or EDF = DFG and DEF = DFG  Examiner's Comments  Candidates have often fou be a challenge and this on A few did give the full and were able to equate two ar property (such as angle DI because they are alternate couldn't construct the full p	e was no exception . correct proof. Some ngles with the correct EF = angle EFH angles) even if they
		Total	6		
18		119 with correct working	5		"Correct working" requires evidence of at least M2 or M1M1

				B3 for $x = 39$ or M2 for $5x = 180 - 22 + 37$ oe or $4x - 37 = 119$ or better or M1 for $4x - 37 + x + 22 = 180$ oe A1 for $x = 39$ AND M1 for $4 \times their x - 37$ or $their x + 22$ If 0 or 1 scored, instead award SC2 for answer 119 with no or insufficient working If 0 scored, instead award SC1 for $[x = ]$ 39	Accept equivalents for M2 e.g. $(180 - 22 + 37) \div 5$ if no algebra seen Accept e.g. $4x - 37$ and $x + 22 = 180$ Using trial, allow correct substitution into $4x - 37 + x + 22$ to imply M1 if 180 also stated  SC marks may be seen on diagram
		Total	5		
19		Angle AEB = angle DEC and [vertically] opposite Angle ABE = angle ECD and same segment Angle BAE = angle EDC and same segment  [Triangle AEB is similar to triangle DEC] [corresponding] angles are equal oe or AAA oe  OR  After two pairs of angles with reasons gives 3 <sup>rd</sup> pair of equal angles with a reason	M2 A1	For M2 only two of the three statements and reasons are required M1 for one pair of angles with a reason  With no errors or incorrect statements seen  If 0 scored, SC1 for at least two correct pairs of angles identified with no / incorrect reasons	Allow any unambiguous labelling for angles e.g. ABE or ABD or B, but not E For reason accept e.g. opp ∠'s For same segment, accept same arc but not same chord Accept 3 <sup>rd</sup> angle in triangle oe for reason with final angle if other two given correctly with correct reasons  Accept they have the 'same/equal angles' oe, AA and similar. Accept symbol ~ for similar  Condone angles

						identified on diagram for <b>SC1</b>
			Total	3		
20			with side 6 cm	2	B1 for a square drawn with side 6 cm or for a square of any length with two diagonals	Mark intention 2 mm tolerance radially on centre point by eye
			Total	2		
21			Accurate ruled perpendicular bisector of BC with two correct pairs of supporting arcs  Accurate ruled bisector of angle ABC with two correct pairs of supporting arcs  Correct position of boat clearly identified at point of intersection of two straight lines	2 2 1 dep	B1 for accurate ruled perpendicular bisector of BC with no or incorrect arcs  B1 for accurate ruled bisector of angle ABC with no or incorrect arcs  Dep on at least B1 and B1	Tolerance ±2 mm and ±2°. Line length at least 2 cm  Tolerance ±2°. Line length at least 2 cm
			Total	5		
22	а	i	[a] 69° and [angles in] alternate segment [are equal]	2	B1 for 69  Response Mark Angles in the alternate se Angles on a tangent which	•
					circle equal the alternate	<u> </u>
		ii	[ <i>b</i> ] 21° [angle between] radius and tangent is 90° <b>oe</b>	1 1	FT 90 – their a (providing the answer is positive)	Condone these terms : diameter,

					perpendicular, right- angle
				Response Mark Angle between tangent at Radius meets tangent at Tangent is perpendicular Tangent and diameter for bisector 1 Tangent subtends a 90 at Angles on a tangent on a Line from centre to tangent the tangent touches the Radius to line SPT will for Angle between tangent at Angle between tangent at Angles at a right angle at Right angle between certangent and Tangent meets the chord	t 90 1 r to radius 1 orm a perpendicular angle at the radius 1 a radius are 90 1(BOD) ent at the point where e circle is 90° 1(BOD) orm a right angle 0 and circle is 90 0 and a straight line is 90 0 dd up to 90 0 otre and tangent 0 l up to 90 0
b	İ	2x [because] angle [subtended] at centre is twice angle at circumference <b>oe</b> 360 – 2x  180 – x	1 1FT 1dep	STRICT FT e.g. 360  - their 2x  Dep on 2x and 360 – 2x  Response Mark  Angles at centre is twice  1  Angles from the same changles on the perimeter  1  Angle at the centre of a contrect the angle at the op Angles at centre is twice	nord are double at the inference 1 are half the centre angle cyclic quadrilateral is sposite point 0
	ii	Opposite angles [in a] cyclic quadrilateral [sum to] 180°	1	Response Mark	

				Opposite angles in a cyclic quadrilateral add up to 180/supplementary 1 Opposite angles in a cyclic quadrilateral = 180 1(BOD) Opposite angles in a quadrilateral add up to 180 0 Angles in a [cyclic] quadrilateral add up to 360 0 It is a cyclic quadrilateral 0 Cyclic quadrilateral theorem 0	
		Total	8		
23	а	115 Corresponding [angles]	2	<b>B1</b> for each	Do not accept F [angles] Ignore irrelevant further comments
	þ	55	3	M1 for 180 – 115 soi  M1 for 60 marked in correct place[s] inside triangle or used in correct calculation to find angle	For M1, accept 65 marked on diagram in correct place[s]  M1 for e.g. 180 – (180 – 115) – 60 oe Do not award if incorrect angle e.g. 65 is also marked in a place where 60 should be
i		Total	5		
24	а	59 alternate segment [theorem]	1 1		condone 'rule' for 'theorem'
	b	46 with correct working	5	B1 for GOH = 44 B1 for OHJ = 44 B2 for [OHG =] 68 or M1 for 180 – 44 [÷2]  If 0 or 1 scored award SC2 for answer 46 with no working or insufficient working Note: If answer is 46	"correct working" requires at least B2 or B1B1  angles may be on diagram  Alt. 1: B1 for GOH = 44 B1 for OGJ = 22 B2 for [OGH =] 68  Alt.2: B1 for

				and the working is incorrect only award the <b>B</b> marks	tangent at H <b>B1</b> for OHJ = 44 <b>M2</b> for 90 - 44
		Total	7		
				<b>M2</b> for a correct method to find the interior angle of a hexagon e.g. $180 - \frac{360}{6}$ or $\frac{(6-2) \times 180}{6}$	"correct working" requires at least M1M1 or M2
				or <b>M1</b> for partial method e.g. $\frac{360}{6}$ or $(6-2) \times 180$	<b>M1</b> implied by 60 or 720
				AND <b>M1</b> for 360 – 90 – their 120	M3 implied by 150
				AND	
25		12 with correct working	6	<b>M2</b> for $\frac{360}{180 - their 150}$ or <b>M1</b> for $180 - their$ 150	<b>M1</b> for ( <i>n</i> – 2)180 = their 150 <i>n</i> oe and <b>M1</b> for a correct rearrangement e.g. 30 <i>n</i> = 360
					Alternative method as the third angle is the sum of the exterior angle of the square and the exterior angle of the hexagon
				If <b>0</b> , <b>1</b> or <b>2</b> scored, instead award <b>SC3</b> for answer 12 with no working or insufficient working	M3 for 90 + $\frac{360}{6}$ [= 150] or M1 for $\frac{360}{6}$ M2 for $\frac{360}{600 - their 60 - 90 - 180}$ oe or M1 for $360 - their 60 - 90 - 180$ oe
		Total	6		
26	а	Ruled bisector of angle DAB to reach CD with construction arcs	2	B1 for correct ruled bisector at least 2	erance ±2°

				cm long by eye with no construction arcs or correct construction arcs with no/wrong bisector drawn	Construction arcs on AB and on AD and two intersecting arcs from these
	b	Arc, centre C, radius 4 cm, intersecting their line once or intersecting BC and CD or two points marked on their line that are 4 cm from C  Locus of line within arc from C rad indicated	2 1dep	B1 for any arc, centre C intersecting their line once or intersecting BC or CD or short arc (at least 1 cm), centre C, radius 4 cm  Dep on at least B1 in (a) and B1 in (b)	Tolerance 3.8 – 4.2 cm Max <b>B1</b> for freehand
		Total	5		
27	a	Using interior angles ((15 – 2) × 180) ÷ 15 or 2340 ÷ 15 seen [Int angle of triangle =] 60 in working 360 – (156 + 60) oe [= 144]	1 1 1	Using exterior angles 360 ÷ 15 seen  [Ext angle of triangle =] 120 in working 24 + 120 [= 144]  Alternative method 1 for 360 ÷ 15 seen 1 for [Int angle of triangle =] 60 in working 1 for 180 – (60 – 24) [= 144]  If 0 scored, SC1 for 24, 36, 60, 120 or 156 shown in correct place on diagram	Mark the working. Mark angles on diagram only if <b>0</b> scored  Working backwards from 144 to 156 [to 15 sides] scores <b>0</b>
	b	10	2		

				M1 for $[n=]\frac{360}{180-144}$ or $\frac{180(n-2)}{n} = 144$	
		Total	5	31 "	
28		45 with correct working	5	B3 for angle BCD = 10 with correct working  Or M1 for angle BAD = 75 or for angle BDE = 180 - 75 or 105  M1 for angle BCD = 18 - their angle BAD  AND  M2 for their angle BCD ÷ 7 × 3 oe Or M1 for their angle BCD ÷ 7 oe  If 0 scored SC2 for answer 45 Or SC1 for angle BCD 105	working" requires at least <b>M1</b> or alternate convincing approach  Angles may be indicated on diagram for part marks
		Total	5		
29		Complete correct argument e.g.  Angle ABC = $20^{\circ}$ [BO =] e.g. $\frac{5}{\sin 10}$ 28.793 or 28.794	B1 M2 A1dep	<b>M1</b> for e.g. $\sin 10 = \frac{5}{[BO]}$ Dep on at least <b>M1</b>	Accept any correct method not using 28.79 Could be on diagram and also accept ABO = 10°, BO'T' = 80°  i.e. BO as subject for M2 and condone sine

					rule with sin 90° for <b>M2</b>
		Total	4		
30		6.67 or 6.670 to 6.671	4	B1 for [BAC =] 45 soi  AND  M2 for BC = S sin (45 or their BAC) sin 58  or  M1 for sin (45 or their BAC) = S sin 58  Examiner's Comments  Lower performing candidate worthwhile progress, as known theorems and the sine rule combined to answer the quantum Angle CAB is 45° from the theorem, although the reast for the award of the mark. common to misuse the theangle as 77°. A few candid was an isosceles triangle as out the angle as 64°.  The sine rule work was perthose attempting to finish to those candidates who had angle CAB were still able to sine rule and so gained two	owledge of circle needed to be uestion.  alternate segment son was not required However, it was orem and give the lates assumed this and therefore worked formed very well by the question. Many of an incorrect value for o use it correctly in the
		Total	4		
31	а	BD = EF or BD = 2t and [opposite sides of a] rectangle [are equal] BC = BD [= 2t] and radii [of a sector/circle]	1	For two marks, 2t must be seen in at least one statement as BD or on the diagram as BD	

				Examiner's Comments  Candidates needed to make clear use of BD as the connection between FE and BC alongside supporting reasons. For example, 'BD = FE because they are opposite sides of a rectangle and so BD = 2t and then BC = BD because they are both radii of the same sector/circle'.  Stated or seen on diagram
	b	ABF = 55 and AB = 5t $\frac{their55}{360} \times 2\pi \times their 5t$ $\frac{35}{360} \times 2\pi \times 2t$ $5t + 2t + 5t + 2t$ $\frac{35}{360} \times 2\pi \times 2t + \frac{55}{360} \times 2\pi \times 5t + 5t + 2t + 5t + 2t$ $\frac{23}{12}\pi t + 14t$	B1 M1 M1 M1 A1	All <b>M</b> marks may be seen within a summarising expression  Condone 10 <i>t</i> + 4 <i>t</i> , 7 <i>t</i> + 7 <i>t</i> etc but not 14 <i>t</i> Part (a) served as a prompt for part (b) and most candidates making an attempt deduced that AB = 5 <i>t</i> , which enabled them to gain a mark if showing the sum of the four straight sides leading to 14 <i>t</i> . Candidates could also gain a mark for having both AB = 5 <i>t</i> and angle ABF = 55°.  The remaining three marks were for the arc lengths of the two sectors and completing the summation of the perimeter to the given answer without error. Some candidates found the areas of the sectors, but then abandoned their work. Generally, those who made an attempt knew what they were doing and completed the task accurately.
		Total	7	
32			1	

ABF	60 equilateral/all angles equal
FBC	120 $_{\rm to}$ straight line/line adds
BCF	add to 180
ECD	60 equilateral/all angles equal
FCE	90 straight line and 180– $30$ – $60$

If <b>0</b> or <b>1</b>	scored,	instead
award		

1

1

1

**SC2** for all of these angles correct in template or on diagram

Accept in any order Condone spelling

Ignore other

angles

If **0** scored, instead award **SC1** for two of the first four angles correct in template or on diagram

> For full marks, must be convinced they are working forwards and not backwards

# **Examiner's Comments**

Marks were given as one mark for each complete, correct, relevant statement. There are five specific angles that need to be found in order to show what the question requires. Other angles (such as FAB and CEF) are not necessary to answer the question and so received no credit. The statements were accepted in any order.

Correct notation was required, such as angle 'ABF' rather than angle 'B'. This question used the command words 'show that', so for the final mark it was a requirement to present the arithmetic 180 – 30 – 60 (or similar) that justifies angle FCE as being a right angle.

Candidates have struggled in the past to present their working and reasons clearly. The provided template appeared to help candidates achieve marks.



#### **Assessment for learning**

Content statement 8.01b of the <u>specification</u> requires standard labelling of angles, such as 'angle ABC'. If there is just one triangle (for example, as is often the case in trigonometry) then 'angle B' is unambiguous, but on diagrams

				like the one presented here, three-letter notation is needed.	
				Exemplar 2	
				Found B. C. and D is on a margin line  - Power B. C. and D is on a margin line  - Trangle A. B. C. and D is on a margin line  - Trangle A. B. C. and D is on a margin line  - Trangle A. B. C. and D is on a margin line  - Trangle A. B. C. and D is on a margin line  - Trangle A. B. C. and D is on a margin line  - Trangle B. C. and D is a sponwage large.  One is margin line in sponwage large.  One is the invariant line in large large.  - Angul B. B. C. and D. C. and L. C. S. S. S. G. D.  Angul B. B. C.	
				There is no credit for the first statement as FAB is not needed to answer the question set. Instead, the candidate should have referenced angle ABF. In the second statement, angle DCE is relevant, 60° is correct and the equilateral triangle reason is correct, and so a mark is given. Likewise, the third and fourth statements are relevant, correct and explained, gaining another mark each. The fifth statement does not receive a mark because angle BFC is not relevant to the question. Finally, angle FCE is justified to be a right angle (or 90°) with a reason and supporting calculation.	
				In total four of the five marks have been given. The mark for angle ABF has not been given as the reason has not been given despite 60° being marked on the diagram.	
				Had their reasons been insufficient or omitted, or incorrect angle notation used, candidates could still receive SC2 or SC1 marks for correct angles marked on the diagram.	
		Total	5		
33	а	115	4	<b>M1</b> for $4x - 150 = 2(x + 20)$ <b>oe M1</b> for $4x - 150 = 2x + $ FT linear eqn with	
				M1 for $4x - 150 = 2x + 40$ FT their 4 term linear more than 4 terms	

				equation with brackets  M1 for x = 95 FT their 4 term linear equation	but not fewer, must have at least two terms in <i>x</i>
				Examiner's Comments  A few candidates were able equation, solve it to find the use this to find the size of a up an incorrect equation, for $4x - 150$ or $x + 20 + 4x - 1$ through mark was available incorrect equation of equivalence of candidates.	e value of x and then angle BCD. Many set or example x + 20 = 50 = 360. A followed for solving an alent difficulty to the
t	0	65 and Opposite angles of a cyclic quadrilateral are supplementary	2	FT 180 – their (a) B1 for 65 FT  or for correct reason  Examiner's Comments  There were some good rescorrect angle and used the language involving a cyclic candidates were given a particular to the language of the language	correct geometrical quadrilateral. A few

					correct angle with an inco using the correct languag geometrical property.	
			Total	6		
34			QMT and [diameter bisects chord] so VT [diameter] is perpendicular to PQ [chord]  [MT is] common  SAS	1 1 1	Examiner's Comments  This was meant to be a part of the conference of the candidates readered to angle QN most candidates put 90° in the candidates	alised they needed to AT in the first part as Instead and most did It these two angles were It denotes the correct term for It shared' being the It many candidates It was the reason for
			Total	3		
					<b>B1</b> for 67	Note: <b>0</b> for 59 (or any other value) and alternate segment Allow for reason: angle between chord and tangent equals angle in opposite segment
35	а	i	[a] 67° and [angles in] alternate segment [are equal]	2	Response Mark  For additional information (J56004) Mark scheme Additional additional downloadable additional scheme Addi	Appendix within
					Examiner's Comments  Some candidates gave th but many of those did not	

				Response Mark For additional informatio	n refer to <b>2023 June</b>
	ii	[b] 23° [angle between] radius and tangent is 90° oe	1 1		Condone these terms : diameter, perpendicular, right- angle
				FT 90 – their a (providing the answer is positive)	
				Students were not told the parallel, so this has been	•
				engles = \$9 . boommo Ol	varrave argies → it
				Exemplar 2	
				Correct geometric prope implication for this quest	-
				Angle a = 67 * because _el	Hernote segrent theorem. It engle RPT.
				Exemplar 1	
				It is well worth spending terms for the circle and le properties. The concepts something that most can difficult. Candidates ofter facts and hope that they ones.	s of circle theorems is didates seem to find n quote random angle
				Assessmen	nt for learning
				reason. The two most co were 59° and 54. For the important terms are 'alte (there were many reason angles'). There were ma using other words, but the	e reason, the two most rnate' and 'segment' ns involving 'alternate ny attempts to explain it

				(J56004) Mark scheme downloadable additional Examiner's Comments  This was answered bette (a)(i), with many candidate from their incorrect answorthe reason often involved line add up to 180' or 'and up to 90'. Some did not up to 90'.	er than Question 17 Ites following through Her to part (a)(i) correctly. Ited 'angles on a straight Higles on a tangent add Hise the term 'radius' so He to tangent' or 'line I', however this reason
b	i	2x [because] angle [subtended] at centre is twice angle at circumference oe $360 - 2x$ $180 - x$	1 1FT 1dep	STRICT FT e.g. 360  - their 2x  Dep. on 2x and 360 – 2x  Response Mark  For additional information (J56004) Mark scheme downloadable additional Examiner's Comments  In the first part many can some of these did not given the correct term for 'cent ones being 'middle' or 'o the term 'circumference' or 'perimeter'. A few wrothe word 'obtuse' in the cangle was given correctly first one. The third angle other two because it was	Appendix within mark guidance.  Ididates did write 2x, but we the reason correctly. lates who did not use re', the most common rigin'. Some did not use and instead used 'edge' to 360 – 2x, not reading demand. The second y more often than the was dependent on the

				few candidates wrote the third angle correctly; a common wrong answer was 180 – 2x.
	ii	Opposite angles [in a] cyclic quadrilateral [sum to] 180°	1	Response Mark  For additional information refer to 2023 June (J56004) Mark scheme Appendix within downloadable additional mark guidance.  Examiner's Comments  Few candidates answered this question correctly, although some did mention a quadrilateral in a circle or even a cyclic quadrilateral and some wrote that the angles of a quadrilateral added up to 360, which is not what this proves.
		Total	8	
36		with side 5 cm	2	B1 for a square drawn with side 5 cm or for a square of any length with two diagonals  Examiner's Comments  Mark intention 2mm tolerance radially on centre point by eye  Examiner's Comments  Most candidates drew a square of the correct size, but it was quite common for the diagonals to be omitted. When drawn, diagonals were usually accurate, passing well within the tolerance of the centre point.  Some candidates seemingly did not know what a plan view was and there were some diagrams of the triangle front elevation, nets and attempts at 3D drawings of the pyramid.  A few candidates did not understand the meaning of the dashed lines on the diagram and drew dashed lines for their square's top and left sides and the top left diagonal.
		Total	2	
37		Accurate ruled perpendicular bisector of AB with two correct pairs of supporting arcs	2 2 1 dep	Use overlay as a guide

Accurate ruled bisector of angle ABC with two correct pairs of supporting arcs

Correct position of boat clearly identified at point of intersection of two straight lines

Put ruler on screen to check 2 cm if needed

**B1** for accurate ruled bisector perpendicular bisector of AB with no or incorrect arcs

Tolerance ±2 mm and ±2°. Line length at least 2 cm Bisector crosses between circles of overlay but does not cut them and perpendicular by eye

**B1** for accurate ruled bisector of angle ABC with no or incorrect arcs

Tolerance ±2°. Line length at least 2 cm Bisector between or on red lines of overlay arcs

Dep on at least **B1** and **B1** 

## **Examiner's Comments**

Constructions is a topic area that candidates of all abilities can often score well on. On this occasion, about a third of the candidates scored full marks and about another third scored 0, which can make quite a difference to the overall outcome for a candidate.

Even though the actual constructions were within a context, many candidates were able to determine what was required and provide the necessary constructions with supporting arcs. There also appeared to be fewer instances of 'false' construction arcs being added to a line that had been drawn by eye.

The perpendicular bisector of AB was constructed particularly well. The 'same distance from AB and BC' was less well understood as requiring an angle bisection. Those bisecting angle ABC usually did so correctly, but a significant number of candidates instead constructed the perpendicular bisector of BC.



# **Assessment for learning**

Construction arcs are an essential part of the

				working. Some candidate erase them or drew them Candidates should be us their constructions and o not wish to be marked.	n very faintly. sing a dark pencil for
		Total	5		
38	а	125 Corresponding [angles]	2	Examiner's Comments  Most candidates were at mark in this part, usually give the correct reason of	ole to score at least 1 for <i>a</i> = 125°. Many did of 'corresponding
				angles'. Common errors they found the answer for to the geometrical reason geometrical reason such co-interior angles.	or angle a and not refer n, or to give an incorrect
				<b>M1</b> for 180 – 125 <b>soi</b>	For M1, accept 55 marked on diagram in correct place[s]
	b	50	3	M1 for 75 marked in correct place[s] inside triangle or used in correct calculation to find angle	M1 for e.g. 180 – (180 – 125) –75 oe Do not award if incorrect angle e.g. 55 is also marked in a place where 75 should be
				Examiner's Comments	
				Many were successful he 50°. Of those that didn't, correctly identify the ang correct position within the usually marked on the di given for this. The most cassume that the triangle an answer of 70° from 18	le 55° or 75° in the e relevant triangle, agram and credit was common error was to is isosceles leading to

				often 30° from 180° – 75 few candidates that mad within an otherwise corre	e arithmetic errors ect method.
				In problems involving an use the given information angles. Do not assume pushapes that are not given as the triangle here being	n to find the missing properties of angles or n in the question, such
		Total	5		
39		Angle AED = angle BEC and [vertically] opposite Angle DAE = angle EBC and same segment Angle ADE = angle ECB and same segment  [Triangle AED is similar to triangle BEC] [corresponding] angles are equal oe or AAA oe  OR  After two pairs of angles with reasons gives 3rd pair of equal angles with a reason	M2 A1	For M2 only two of the three statements and reasons are required  M1 for one pair of angles with a reason  With no errors or incorrect statements seen  If 0 scored, SC1 for at least two correct pairs of angles	Allow any unambiguous labelling for angles e.g. DAE or DAC or A, but not E  For reason accept e.g. opp ∠'s  For same segment, accept same arc but not same chord  Accept 3 <sup>rd</sup> angle in triangle oe for reason with final angle if other two given correctly with correct reasons  Accept they have the 'same/equal angles' oe, AA and similar. Accept symbol ~ for similar  Condone angles identified on diagram for SC1

				identified with no / incorrect reasons
				Examiner's Comments  This question proved challenging for all candidates and was omitted by a number of candidates.  A few realised that finding equal pairs of angles was the strategy.  More able candidates attempted to work systematically, line by line, giving a pair of angles with a reason.  Angle AED = angle BEC with the reason, [vertically] opposite, earned partial credit for some candidates, but the majority were unable to give correct geometric reasons for the other equal pairs of angles.  A number gave incorrect angle pairs, such as angle A = angle C, perhaps thinking they were alternate angles. Some also referred to lengths
l.		Total	3	and gave reasons of congruency, such as SAS.
40	а	53 alternate segment [theorem]	1 1	condone 'rule' for 'theorem'  Examiner's Comments  The correct answer of 53 was seen quite regularly, the alternative answer often seen was 49. Many candidates did not know the reason and a common response was 'alternating angles'.
	b	38 with correct working	5	B1 for OGH = 52 B1 for JHG = 26 B2 for [OGJ =] 64 or M1 for 180 - 52 [÷2]  If 0 or 1 scored award SC2 for answer 38 with no working or insufficient working  "correct working" requires at least B2 or B1B1  angles may be on diagram  Alt. 1: B1 for JHG = 26

				Note: If answer is 38 and the working is incorrect only award the <b>B</b> marks.	<b>B1</b> for OJH = 26 <b>B2</b> for [OJG =] 64 Alt.2: <b>B1</b> for tangent at G <b>B1</b> for OGH = 52 <b>M2</b> for 90 - 52
				right angles and also ass 52°. The other incorrect triangle GHJ was isosce 104 from which they wor correctly stated that angle some noticed that triang and that angle OGJ was difficult angle to see was half of 52.  Misconcep  Angles that look like right to be right angles. Triangles.	ne answer of 38 which his was only correct if G. Many assumed the ersects the line OG were sumed angle OGJ was assumption was that les and angle JGH was leo OGH was 52° and leo OJG was isosceles therefore 64°. The most is that angle GHJ was
		Total	7	may not be isosceles.	
41		10 with correct working	6	M2 for a correct method to find the interior angle of a pentagon e.g. 180 – (5-2)×180 or M1 for partial method e.g. (5 – 2) × 180  AND  M1 for 360 – 2 × their 108  AND	"correct working" requires at least M1M1 or M2  M2 implied by 108  M1 implied by 72 or 540  M3 implied by 144  M1 for $(n-2)180 = their144n$ oe and M1 for a correct rearrangement e.g. $36n = 360$

**M2** for  $\frac{360}{180-their144}$ 

or **M1** for 180–*their* 144

If **0**, **1** or **2** scored, instead award **SC3** for answer 10 with no working or insufficient working

Alternative method as the third angle is the sum of the two exteriors of the pentagons M3 for  $2 \times \frac{360}{5}$  [= 144] or M1 for  $\frac{360}{5}$  and

for  $\frac{360}{5}$  and  $\frac{360}{5}$  for  $\frac{360}{360-their_{144-180}}$  oe or M1 for  $360-their_{144-180}$  oe or -180 oe

#### **Examiner's Comments**

The first error was that some candidates thought that a pentagon had either 6 or 8 sides. There are two distinct methods to find the internal angle of a polygon. The first method involves

using the formula for the angle sum, n
However this is very cumbersome to use when you have the angle and you need to find the number of sides. The other method involves finding the external angle first and in one step it

is 2 Most candidates, using either method, found the internal angle of their pentagon correctly and most of these found the third angle round the point. However some candidates did not know how to find the number of sides from the internal angle of the third polygon. In this question the working was not always easy to follow.

## Exemplar 1

$$\frac{360}{5} = 72$$

$$108 \times 180 - 72 = 108$$

$$108 \times 2 = 216$$

$$360 - 216 = 144$$

$$180 - 144 = 31$$

$$\frac{360}{34} = 10$$

The method is logical and easy to follow. The first two steps are labelled "ext. angle" and "int. angle". They find the number of sides by reversing the first two steps. This demonstrates that, in this question, this method proved to be easier than the other method as demonstrated in Exemplar 2.

		Total	6	10 00	formula to find the ngle sum and it is more ht is the angle sum $5-2$ which shows to below top right is the ar pentagon and below the point. They find it la to find the number of right, they appear to heck it. However this is
42	а	Ruled bisector of angle ABC to reach CD with construction arcs	2	B1 for correct ruled bisector at least 2cm long by eye with no construction arcs or correct construction arcs with no/wrong bisector drawn  Examiner's Comments  Many candidates did not distance from side AB ar the bisection of angle B.	interpret "the same
	b	Arc, centre C, radius 5 cm, intersecting <i>their</i> line twice or intersecting BC and CD or two points marked on <i>their</i> line that are 5 cm from C Locus of line within arc from C rad indicated	2 1dep	B1 for any arc, centre C, intersecting their line at least once or intersecting BC or CD or short arc (at least 1	Tolerance 4.8 – 5.2 cm Max <b>B1</b> for freehand, all within template

		Total	5	cm), centre C, radius 5 cm  Dep on at least B1 in (a) and B1 in (b)  Examiner's Comments  In this part, the bench w path, represented by the candidates who produce constructions in (a) and rather than indicating pa	as to be placed on the angle bisector. Most ed the correct (b) then shaded a region
				Using exterior angles:	
43	a	Using interior angles: $((10-2)\times 180)\div 10 \text{ or } 1440\div 10$ seen [Int angle of triangle =] 60 in working $360-(144+60) \text{ oe } [=156]$	1 1 1	360 ÷ 10 seen  [Ext angle of triangle =] 120 in working  36 + 120 [= 156]  Alternative method:  1 for 360 ÷ 10 seen 1 for [Int angle of triangle =] 60 in working 1 for 180 – (60 – 36) [= 156]  If 0 scored SC1 for 24, 36, 60, 120 or 144 shown in correct place on diagram	Mark the working. Mark angles on diagram only if 0 scored.  Working backwards from 156 to 144 [to 10 sides] scores 0
				Examiner's Comments  AfL	<u>i</u>
				Candidates were require marked on a diagram wa question, it is important convinces the examiner demonstrate each step a backwards from the give	as 156°. In a "show" that the candidate that they can

	b	15	2	144 + 60 = 204 and 360 equivalents.  M1 for $[n =]$ $\frac{360}{180-156}$ or	table. Instead, 144 rived, for example from n then be completed by
				$\frac{180(n-2)}{n} = 156 = 156$	
		Total	5		
44		44 with correct working	5	B3 for angle BCD = 110 with correct working or M1 for angle BAD = 70 or for angle BDE = 180 – 70 or 110 M1 for angle BCD = 180 – their angle BAD  AND  M2 for their angle BCD ÷ 5 × 2 oe or M1 for their angle BCD ÷ 5 oe  If 0 scored SC2 for answer 44 or SC1 for angle BCD = 110	For full marks "correct working" requires evidence of at least M1 AND M1 ie at least a correct angle and some ratio work Ignore geometric reasons if given  For B3 "correct working" requires at least M1 or alternate convincing approach  Angles may be indicated on diagram for part marks  May be seen on diagram
		Total	5		
45		complete correct argument e.g. angle ABC = $40^{\circ}$ [BO = ] e.g. $\frac{6}{\sin 20}$ 17.542 or 17.543	B1 M2 A1dep	<b>M1</b> for e.g sin $20 = \frac{6}{[BO]}$ <b>dep</b> . on at least <b>M1</b>	accept any correct method not using 17.54 could be on diagram and also accept ABO = 20°, BO'T' = 70° i.e BO as subject for M2 and condone sine

			rule with sin 90° for <b>M2</b>
	Total	4	